



# Modeling Cosmic Ray Electrons in the Multiphase ISM

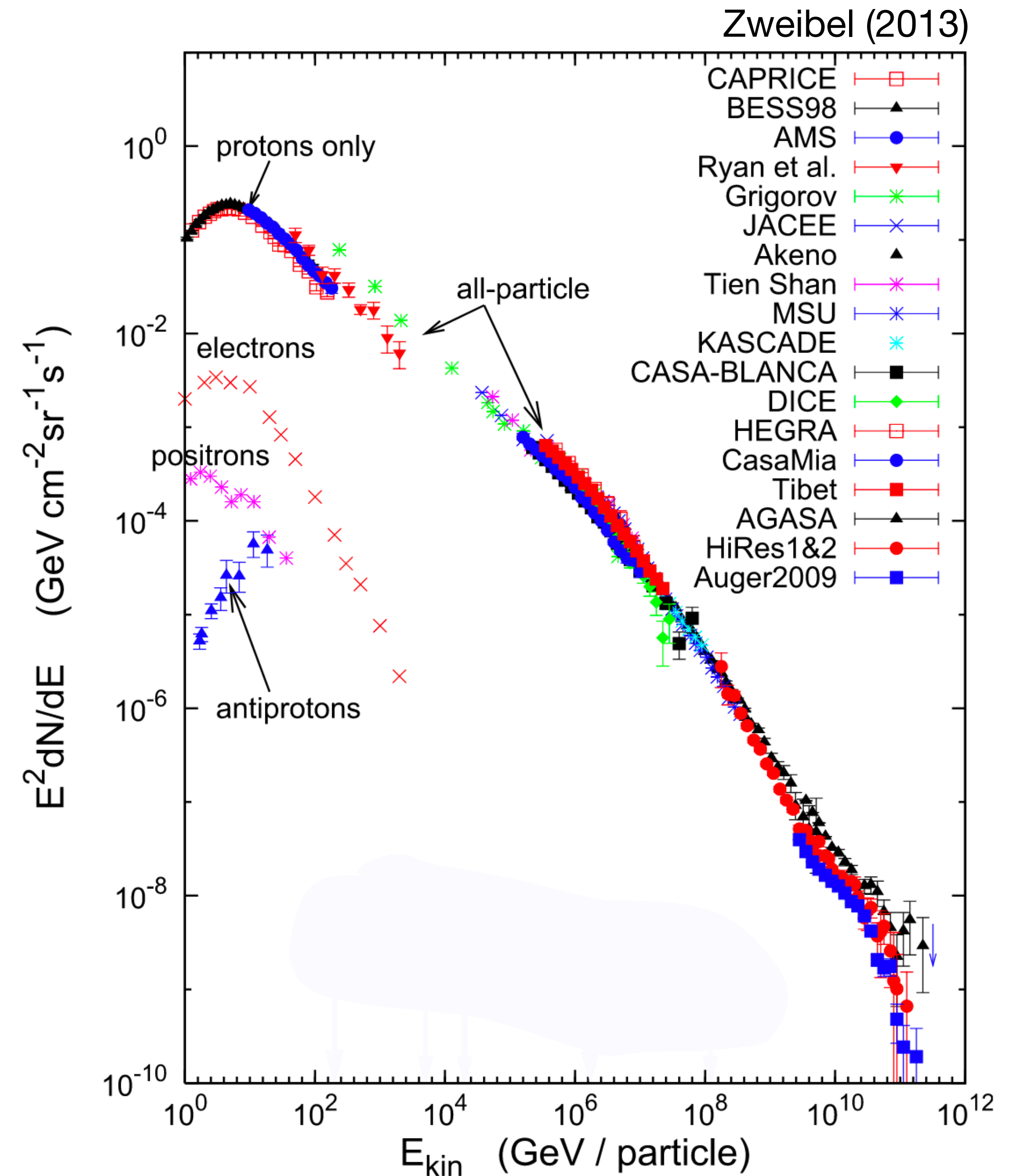
Nora Linzer, October 24, 2024

With Lucia Armillotta, Eve Ostriker, and Eliot Quataert

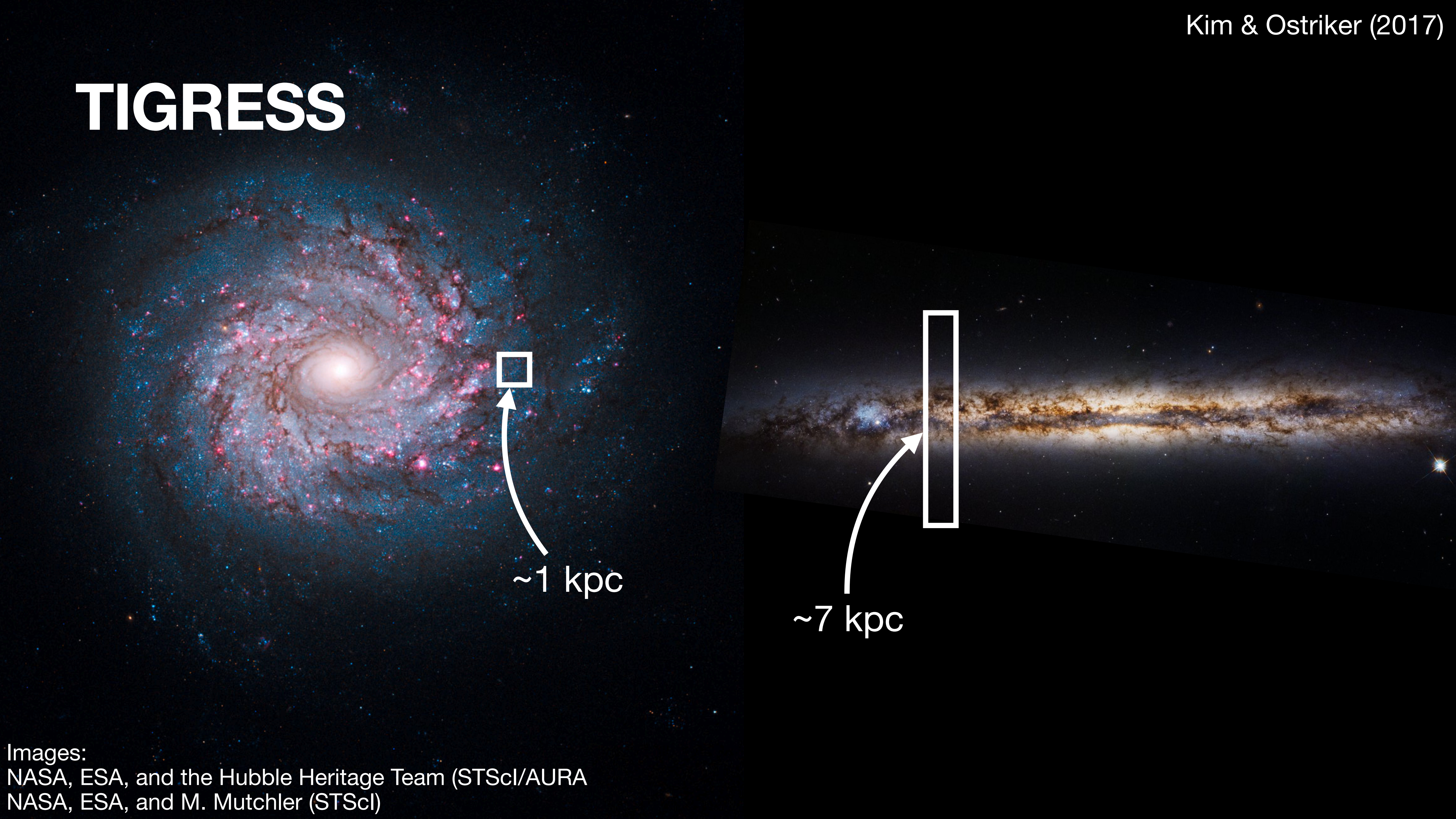
Image: Ruszkowski and Pfrommer, 2023

# Why model electrons?

- Unlike protons, do not impact the gas dynamically
- Visible in **synchrotron radiation**  
→ key tracer of the CR population where protons are not detectable
- From radio observations, learn about:
  - CR electron spectrum
  - CR proton spectrum
  - Magnetic field



# TIGRESS



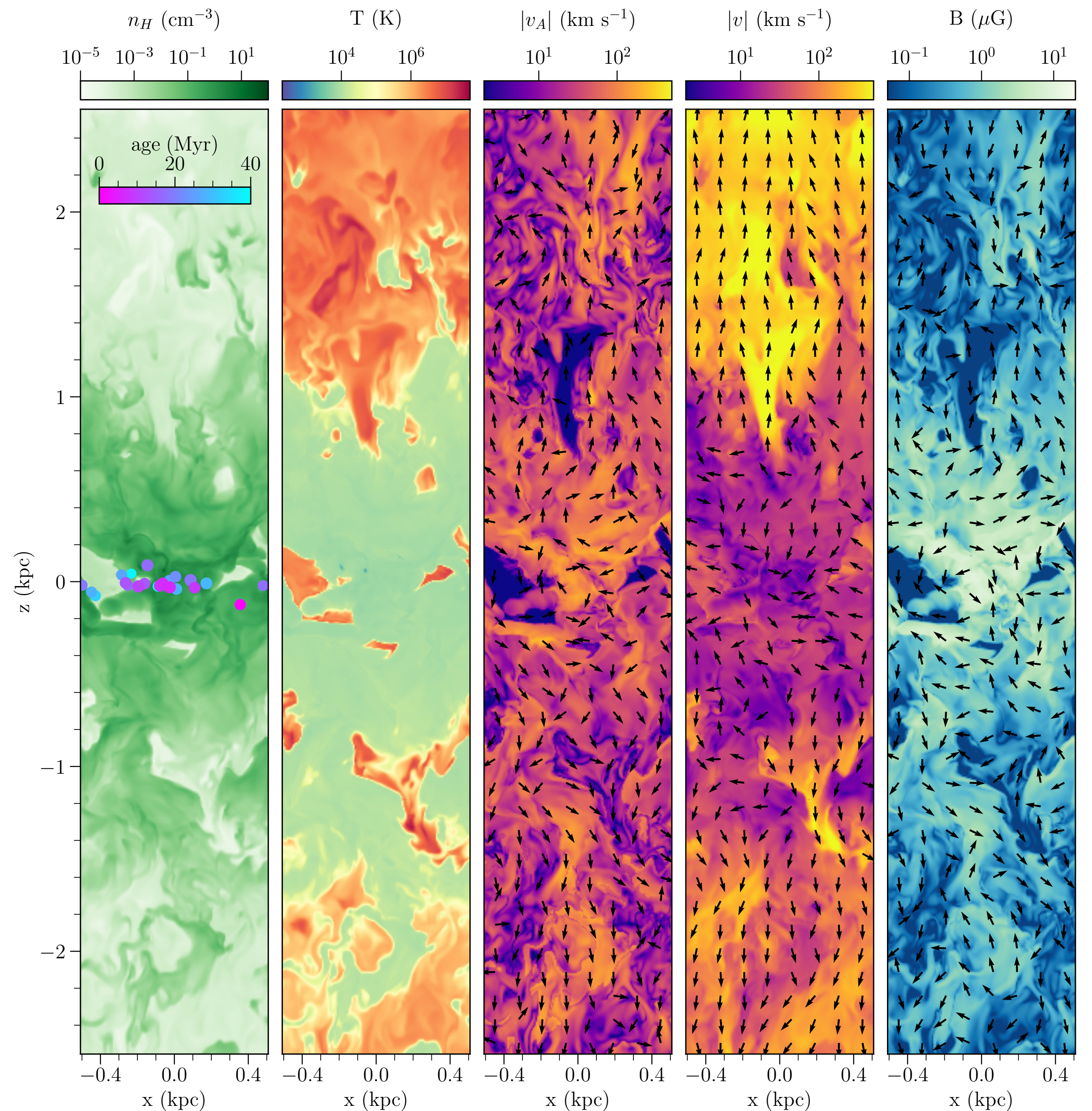
~1 kpc

~7 kpc

# Modeling CRs in TIGRESS

See Jiang & Oh (2018) + Armillotta et al. (2021)

1. **Injection** around star particles
2. **Transport** including:
  1. **Advection** with the gas
  2. **Streaming** along magnetic fields
  3. **Diffusion** relative to the magnetic fields
3. Energetic **losses** through interactions with the local ISM



# Streaming Coefficient

CRs scatter off of Alfvén waves generated by the streaming instability — the **self-confinement** model

$\Gamma_{\text{stream}} = \Gamma_{\text{damp}}$

The diagram features the equation  $\Gamma_{\text{stream}} = \Gamma_{\text{damp}}$  centered at the top. Two curved arrows originate from below the equation. One arrow starts under the  $\Gamma_{\text{stream}}$  term and points to the text 'Depends on local CR properties'. The other arrow starts under the  $\Gamma_{\text{damp}}$  term and points to the text 'Either ion-neutral or non-linear Landau damping, value depends on local gas properties'.

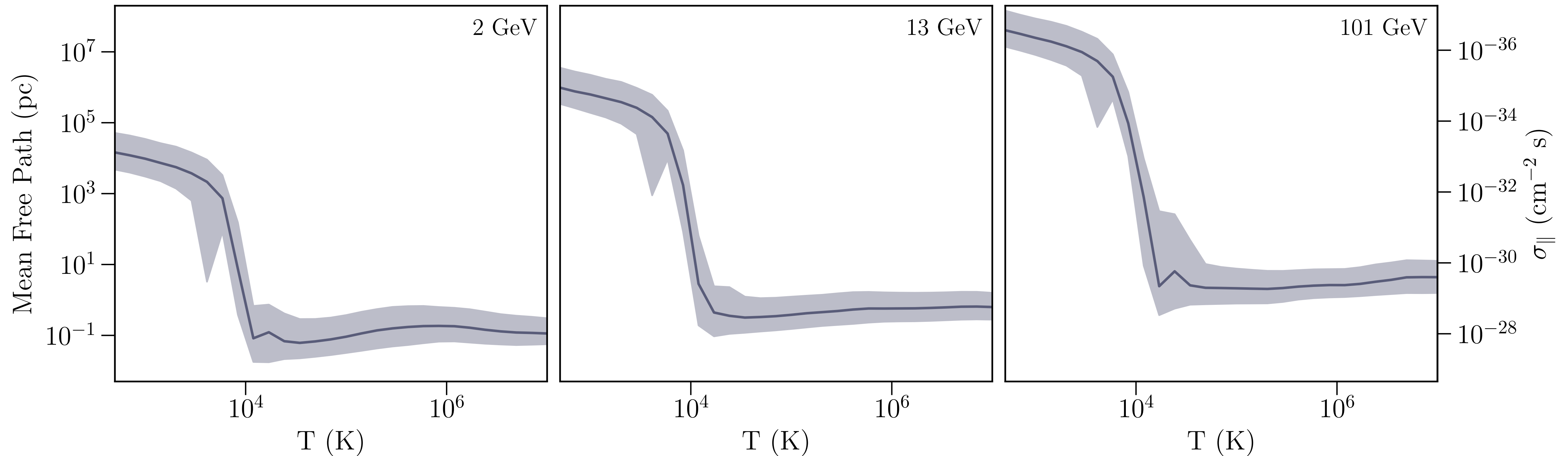
Depends on local CR properties

Either ion-neutral or non-linear  
Landau damping, value depends  
on local gas properties

# Streaming Coefficient

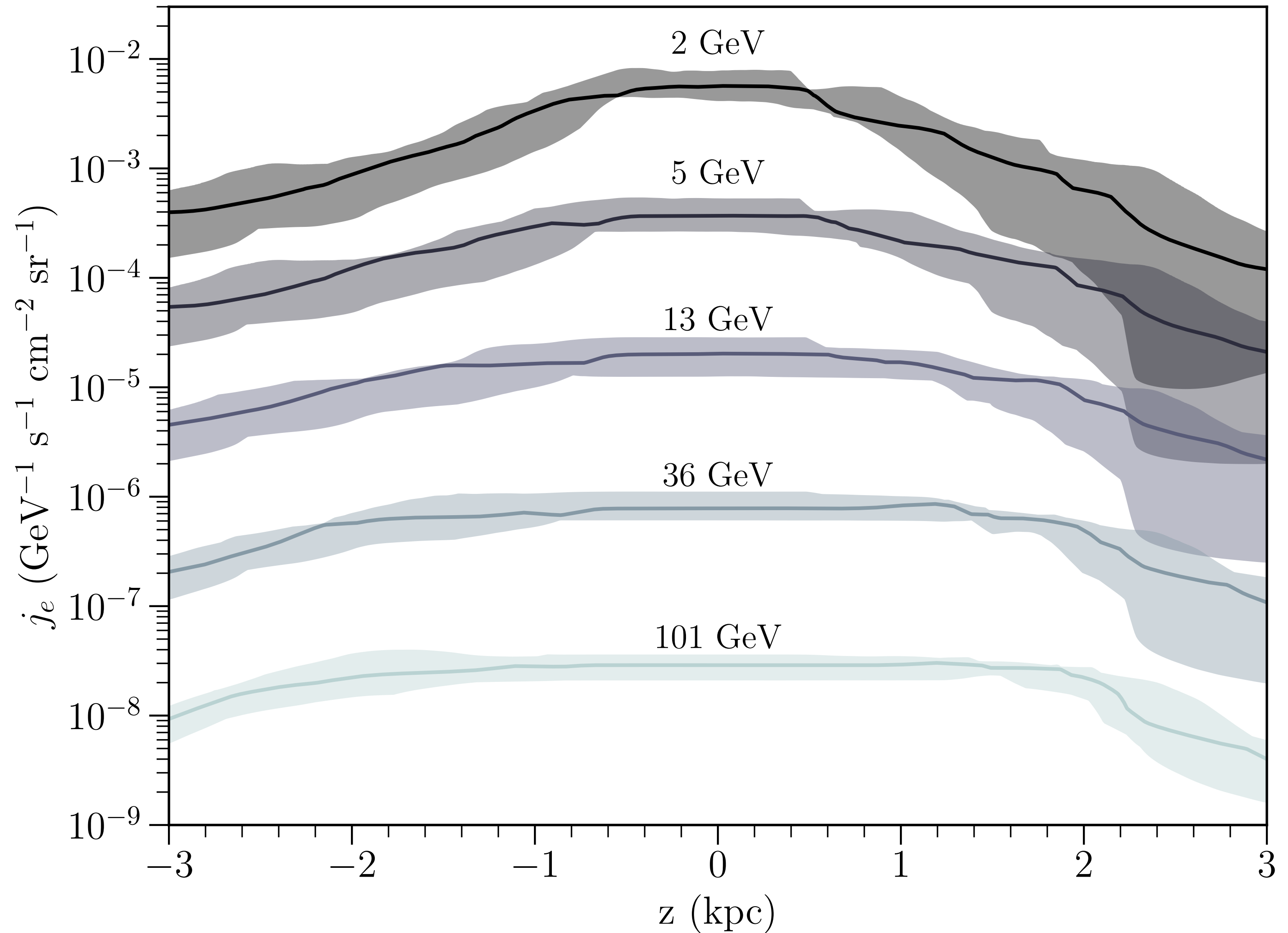
CRs scatter off of Alfvén waves generated by the streaming instability — the **self-confinement** model

$$\Gamma_{\text{stream}} = \Gamma_{\text{damp}} \rightarrow \sigma_{\parallel}$$



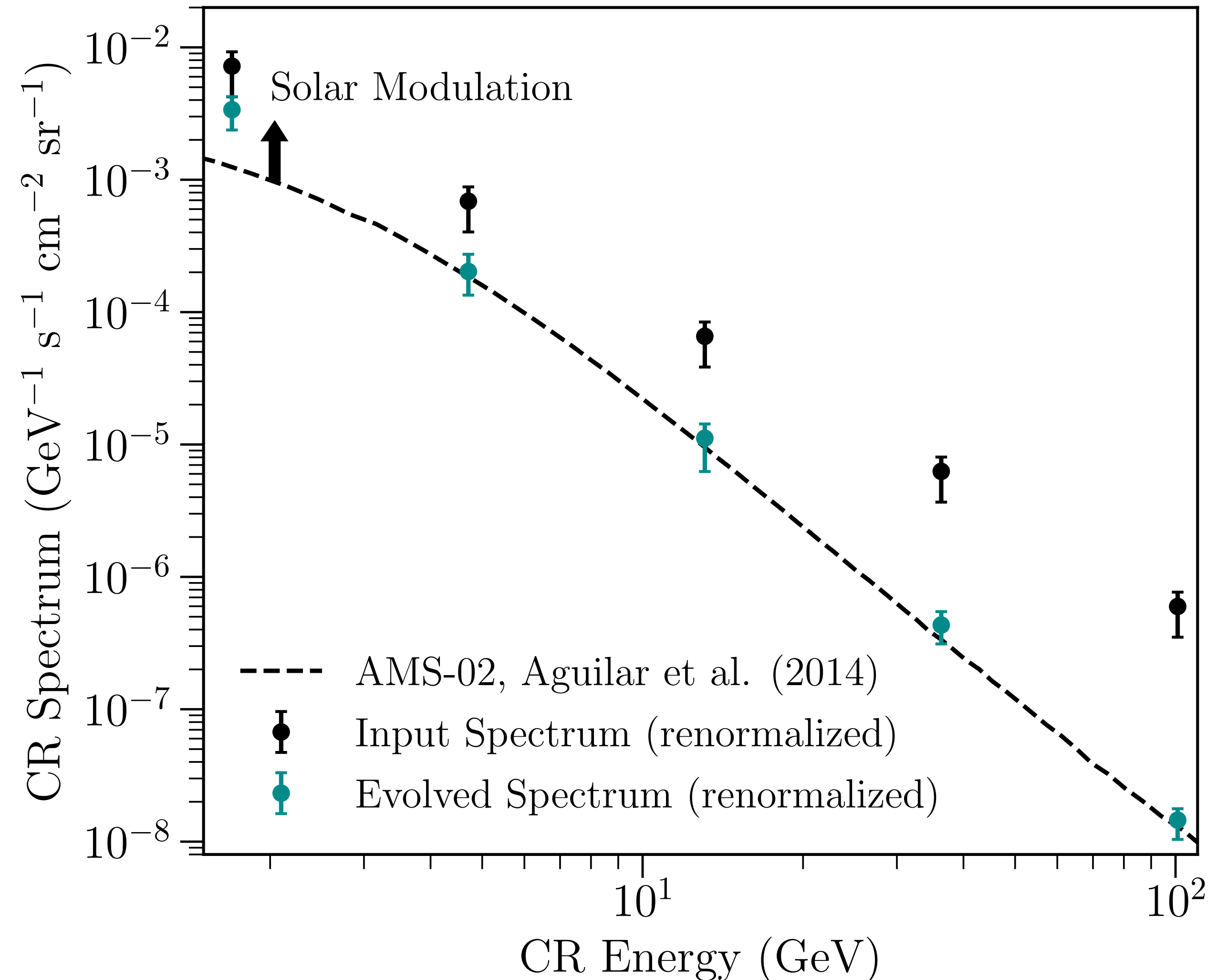
# Vertical Profiles

- Horizontal average of the CRE spectrum at each energy
- The scale height of the CRs becomes larger at higher energies



# CR Electron Spectrum

- We inject CR electrons with a fixed power law slope,  $j_e \propto E^{-2.3}$
- Through their evolution, the electrons experience energy dependent spectral steepening due to diffusion and losses
- The final spectrum is in excellent agreement with direct observations



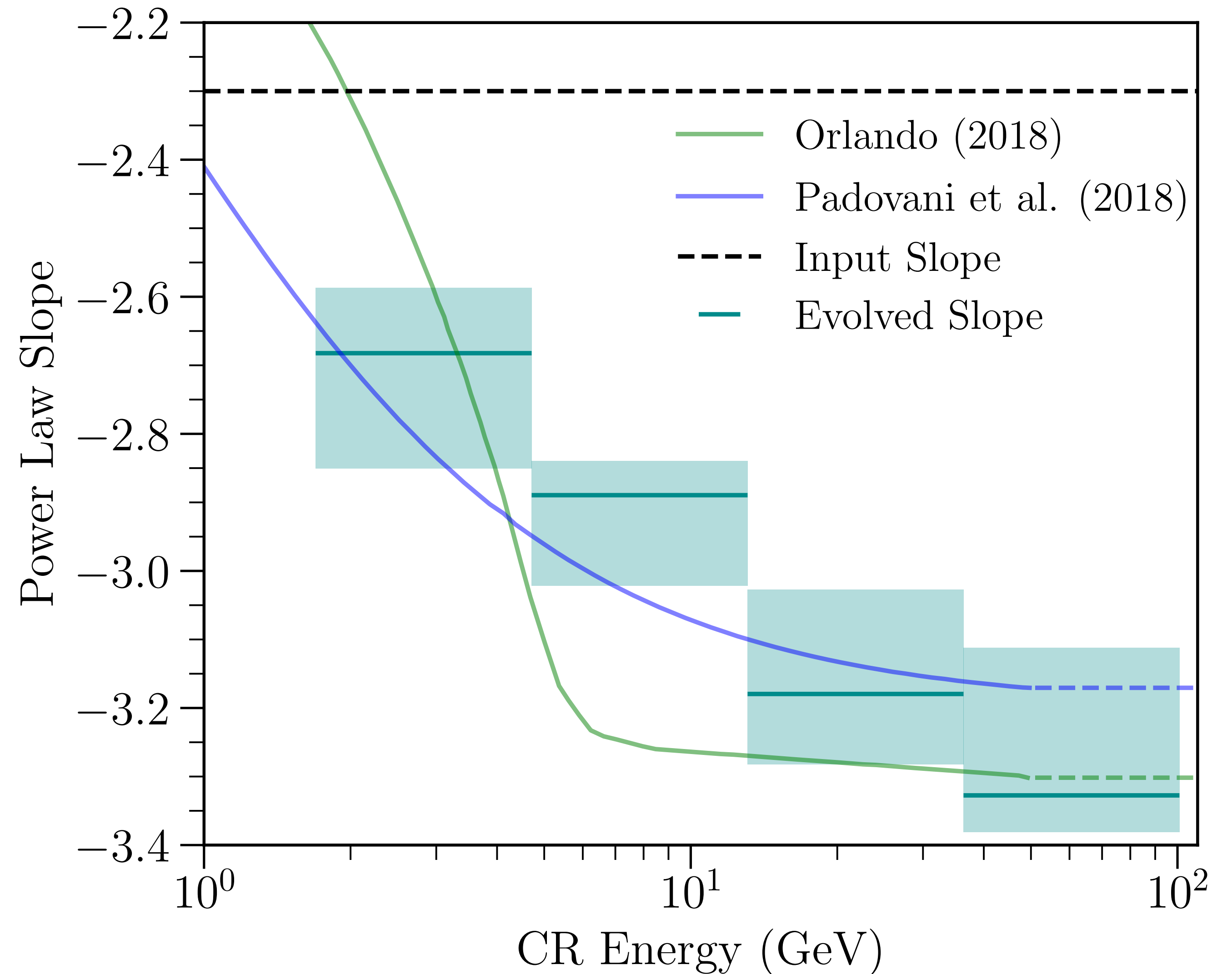


# Power Law Slope

- Compare power law slope of the simulated spectrum to values based on observations

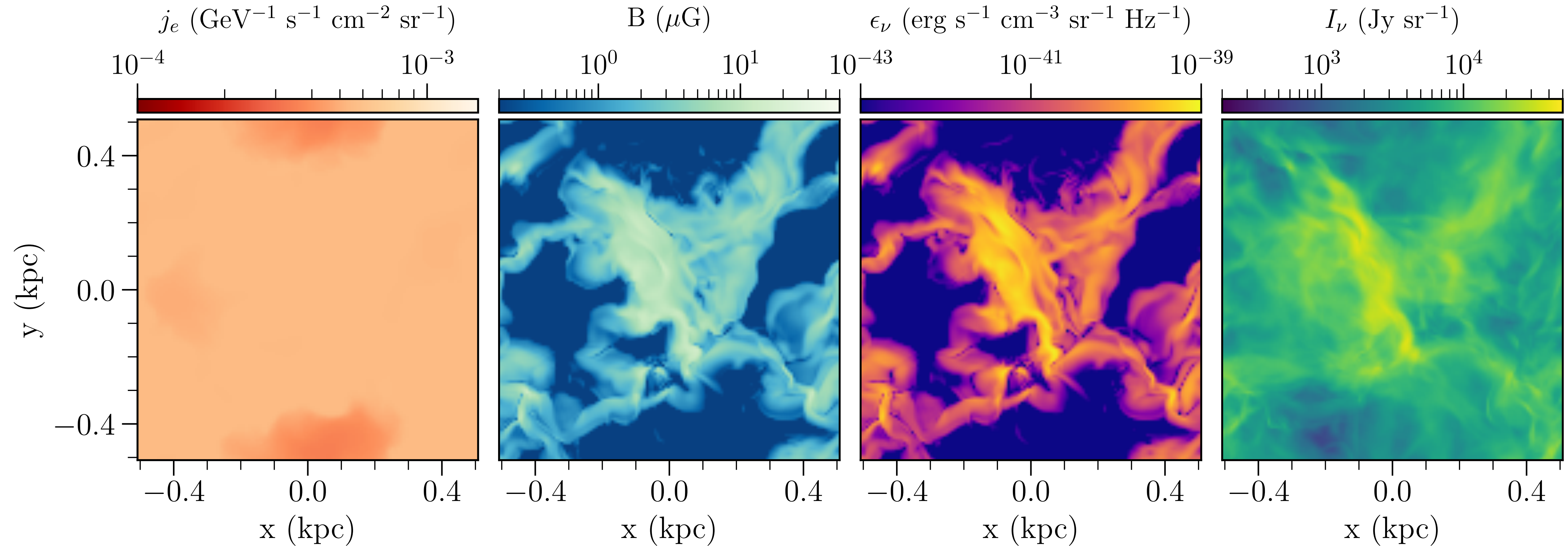
$$s = \frac{d \log j_e}{d \log E}$$

- As is observed, we find the electron spectrum not to be well represented by a single power law



# Synchrotron Emission

$$\epsilon_\nu \propto \int j_e(E) P_\nu(E, B) dE$$



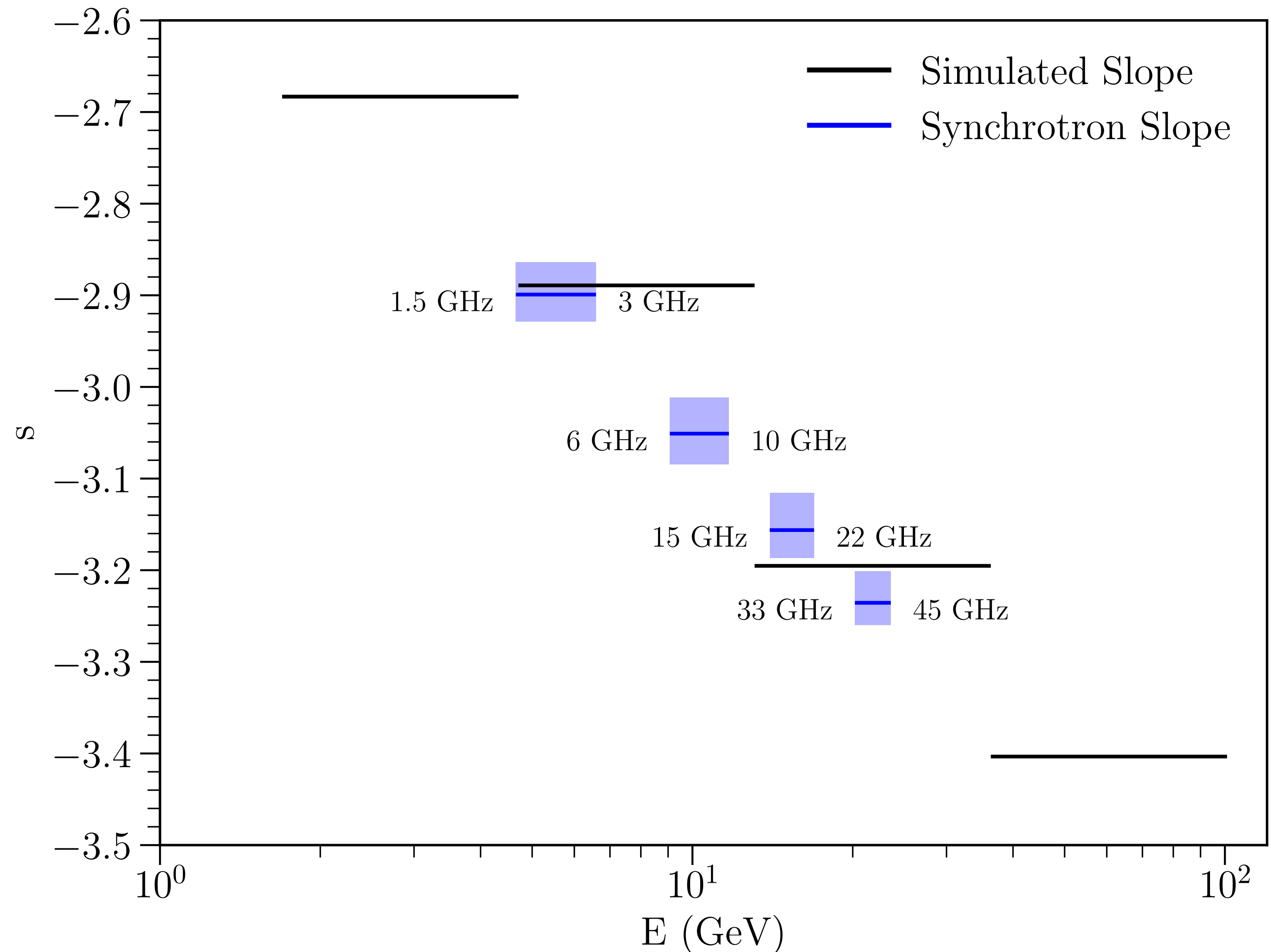
# Estimated Slope

We estimate the CR spectral slope from the radio spectrum:

$$I_\nu \propto \nu^\alpha \rightarrow \alpha = \frac{\log(I_{\nu_1}/I_{\nu_2})}{\log(\nu_1/\nu_2)} = \frac{s + 1}{2}$$

The energy of CRs responsible for emission at frequency,  $\nu$ , is given by:

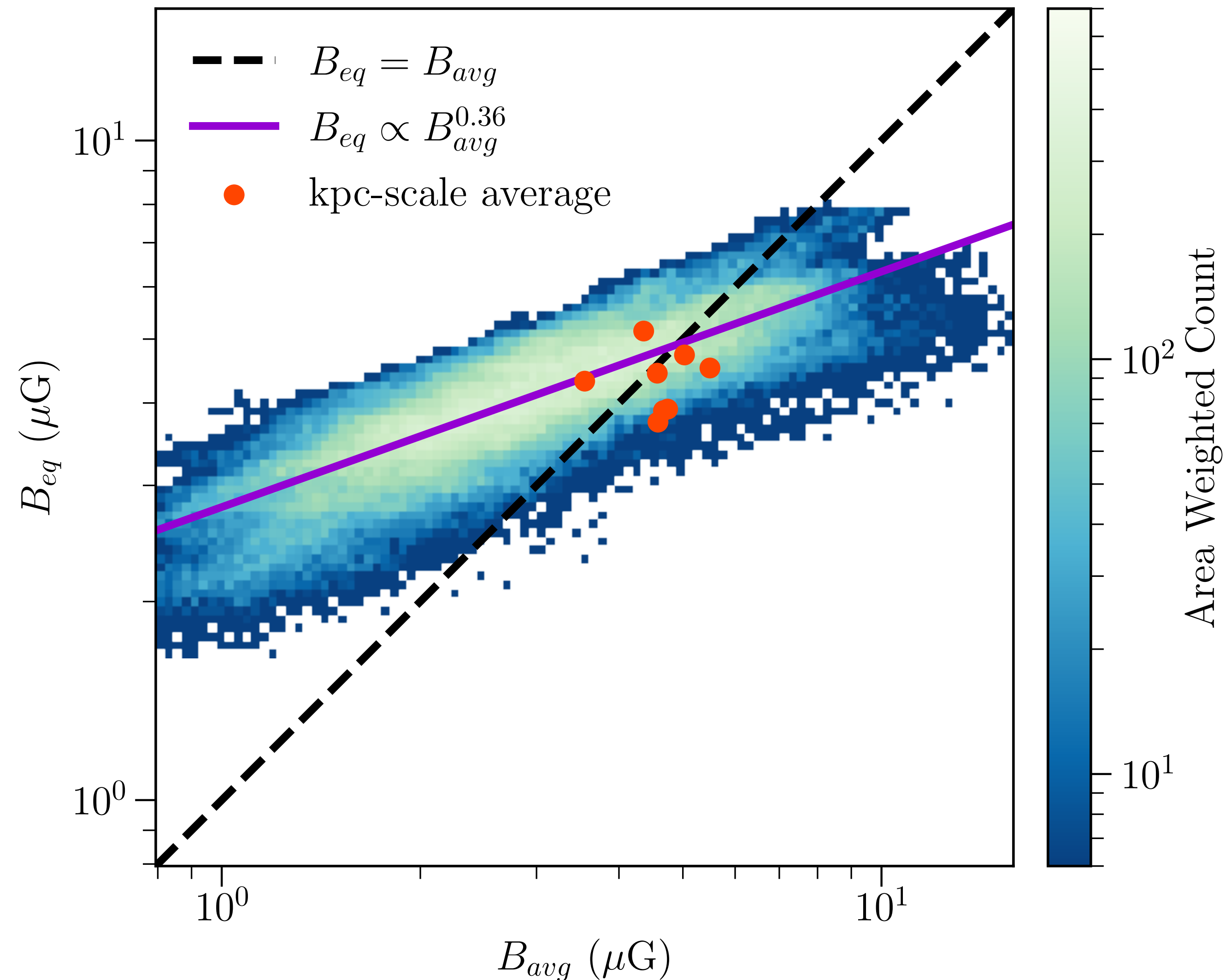
$$E \approx 8 \text{ GeV} \sqrt{\left(\frac{\nu}{\text{GHz}}\right) \left(\frac{B_\perp}{\mu\text{G}}\right)}$$



# Equipartition Estimate

$$B_{eq} \propto \left[ \frac{(\mathbf{K}_0 + 1)}{Lc_4(i)} \times I_\nu \right]^{\frac{1}{\alpha + 3}}$$

- The equipartition estimate of magnetic fields is a function:
  - Synchrotron intensity
  - Radio spectral index
  - Scaling factors
- Although the estimate may work well on ~kpc scales, it breaks down at smaller scales



# Conclusions

- ▶ We reproduce the observed CR electron spectrum between 1-100 GeV using the self-confinement model of CR transport.
- ▶ The CR spectral slope can be recovered from synchrotron observations.
- ▶ Although the equipartition estimate of magnetic fields is a good approximation on kpc scales, it may not hold on smaller scales.